

LIST OF SYMBOLS

C_p	Performance coefficient of wind turbine
f	Supply frequency, (Hz)
i_b	Boost converter inductor current, (A)
i_{dg}, i_{qg}	dq PMSG stator current components, (A)
i_a, i_b, i_c	Three phase grid currents, (A)
i_d, i_q	dq axis components of grid currents, (A)
i_d^*, i_q^*	dq reference grid current components, (A)
i_s	PMSG supply current, (A)
i_c	Magnetic amplifier control winding current, (A)
I_{inv}	Inverter IGBT current, (A)
I_{rec}	Rectifier diode current, (A)
L_l	Booster inductance, (H)
L_d, L_q	PMSG dq axis inductances, (H)
P_w	Power absorbed by windmill, (W)
P_{Grid}, Q_{Grid}	Grid active and reactive power, (W, VAR)
P_{Gen}, Q_{Gen}	PMSG active and reactive power, (W, VAR)
R_a	Stator armature resistance, (Ω)
R	windmill blade radius, (m)
T_e	Electromagnetic torque, (N.m)
V	Wind velocity (m/s)
V_{inv}	Inverter IGBT voltage, (V)

v_b	Input capacitor voltage of boost converter, (V)
v_{dc}	DC link capacitor voltage, (V)
V_{rec}	Rectifier diodes reverse voltage, (V)
v_a, v_b, v_c	Three phase grid voltages, (A)
β	Blade pitch angle (BPA), degree
δ	Load angle, between q -axis and phase 'a' voltage, (rad)
ϕ_f	Permanent magnet flux linkage, (Wb)
ϕ_d, ϕ_q	dq axis flux-linkages, (Wb)
θ	Phase angle of grid voltage, (degree)
λ	Tip-speed ratio (TSR)
ρ	Air density
ω	Electrical rotor angular speed, (rad/s)

I. INTRODUCTION

The increasing consumption of the traditional fossil energy raises problems such as global warming, pollution and energy security. Renewable energy sources are the most promising alternative energy in future. With the increasing penetration of wind energy and the improvement of its technology make it important to carefully reconsider the operating characteristics of wind farms, especially during grid fault conditions. Previously, disconnection of distributed generators (DGs) if one of the parameters (e.g. voltage, frequency, etc.) was beyond or below the permissible band was not a problem as the installed DG capacity was low. However, with installed mega watt (MW) of wind power, disconnection of the DG is no longer valid. Disconnection of many wind turbines (WT) during fault and evoked loss of a large share of generation can be dangerous for the stability of the power system operation. Thus, new connection requirements for DG units have been introduced by many system operators [1]. For these reasons, wind turbines are expected to behave like conventional synchronous generators during voltage dips, remaining connected and supplying reactive power during and after the voltage dip. For example, the LVRT requirement for the UK electrical grid is shown in figure (1) [2], where the wind turbine has to remain connected to the network for grid faults that last up to 140 ms and upon the restoration of voltage to 90% of nominal.

During normal operation of WT and with the absence of grid voltage dips, the wind energy conversion system (WECS) extracts maximum power from the wind regardless of wind speed. The turbine controller achieves the maximum power point tracking (MPPT) algorithm [3-5]. The extracted power passes through stages of power electronic conversions and connected to the grid at the end. When a network fault occurs, the wind turbine DC link voltages rise rapidly as the WT grid side converter is prevented from transmitting the active power coming from the generators. Therefore, to maintain the wind turbine DC link voltage below its upper limit, either dissipating the excess power or reducing the generator power is mandatory.

Methods for LVRT capability enhancement and overcoming the rise in DC link voltage vary according to the turbine variables and utility grid variables. To enhance the LVRT capability for WT, blade pitch angle control can be used as in [6] through shifting the WT blades from an angle where it extracts maximum power to another angle of attack, thus reducing the amount of power being extracted from the wind and compensating the rise in the DC link voltage. Another suggested solution is to oversize the DC link capacitor to compensate for the DC link voltage rise during grid dips as in [7]. Active crow bar technique is considered one of the mostly used solutions for LVRT. By the insertion of a resistor in the dc link controlled by a power electronic switch, excess energy is dissipated and a balanced power flow is restored [8]. Other methods for LVRT improvement can be through de-loading of the wind turbine as demonstrated in [9] by the proper control of generator side converter, grid side converter control. The former controls the generator electromagnetic torque by controlling the generator armature current while the latter maintains the DC link voltage constant by controlling the grid side converter [10]. VAR and voltage compensation (shunt/series, shunt & series) has been one of the effective techniques in enhancing the LVRT capability on a larger scale such as wind farm level at the point of common coupling. VAR compensators employ the use of Static VAR Compensators (SVC), STATCOM, Magnetic Energy Recovery Switch (MERS), Dynamic Voltage Restorer (DVR) and Thyristor Controlled Series Capacitor (TCSC) [11-15].

This paper proposes a novel topology that can be used to enhance the LVRT capability for PMSG grid connected wind turbines. The topology is based on series voltage compensation using magnetic amplifiers. Magnetic amplifier has been known for years and is used in variety of applications such as position control. It is a device which acts as a variable inductance if inserted between a source of emf and a load. Through proper control of its control winding current, magnetic amplifier will eventually act as a current limiter and a series voltage compensator at the event of transient voltage dip to enhance LVRT capability. The basic principles of magnetic amplifiers design considerations are demonstrated to show the effectiveness of magnetic amplifier in reducing the DC link voltage rise as well as limiting the stresses on the power electronic converters in case of grid voltage dips.

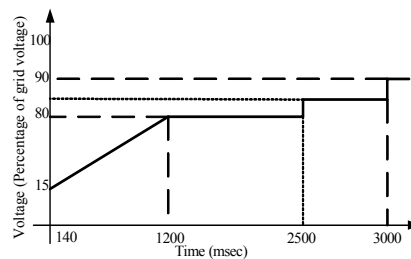


Figure 1: British Grid Code for Fault Ride Through

II. SYSTEM CONFIGURATION

A. System Modeling:

The WECS employed for grid connection of PMSG wind turbine is found in figure (2) which consists of the drive train, PMSG, diode bridge rectifier, boost converter circuit and a voltage source inverter (VSI). As mentioned earlier, MPPT is one of the essential features of grid connected WT. The techniques used for PMSG WT are vast and diverse. One of the oldest approaches is the tip speed ratio (TSR) technique, where the turbine pitch angle is regulated according to the measured wind speed. TSR's main disadvantage lies in the cost of the anemometers used as well as its low accuracy in the presence of wind gusts [16]. Hill climbing search technique (HCST) is another method for MPPT, where the PMSG shaft speed is perturbed in small steps while observing the wind turbine mechanical power [17, 18]. The disadvantage of HCST lies in the slow responses to wind changes as well as oscillation around the optimum point making the HCST suitable for small-scale WT. Finally, optimum relationship based (ORB) MPPT, is the most popular technique used with large scale WT. Lookup tables are recorded with stored values of optimal generator speed and the corresponding maximum power (or maximum torque) at various wind velocities. ORB requires system pre-knowledge and many field tests to obtain accurate optimal relation between system parameters [19-21].

In the absence of LVRT enhancement methodology, grid voltage dips can cause a serious rise in the DC link voltage which might lead to the destruction of the power converters. To demonstrate this effect, figure (2) shows the block diagram being used in the simulation analysis of a 1.5MW grid connected PMSG WT whose parameters can be found in table (1). System description is presented in the following sections.

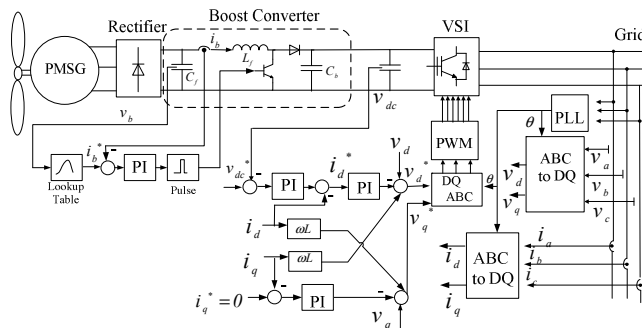


Figure 2: Block diagram for system under investigation

1) Wind Turbine Model:

The power absorbed by windmill from air, P_w , is given by (1)

$$P_w = \frac{1}{2} \rho \pi R^2 V^3 C_p \quad (1)$$

When wind velocity is invariable, the power P_w is directly proportional to C_p .

$$\lambda = \frac{\omega R}{V} \quad (2)$$

$$C_p = 0.73 \left(\frac{151}{\lambda_1} - 0.58\beta - 0.2\beta^{2.14} - 13.2 \right) e^{-\frac{18.4}{\lambda_1}} \quad (3)$$

$$\lambda_1 = \frac{1}{\left(\frac{1}{\lambda - 0.02\beta} - \frac{0.08}{\beta^3 + 1} \right)} \quad (4)$$

Table 1: PMSG DATA [22]

Parameter	Value
Base power (MVA)	1.5
Base voltage (V)	690/√3
Base frequency (Hz)	11.5
Pole pairs of PMSG	40
PMSG inertia constant (pu)	0.5
Shaft stiffness (pu)	2
Rated generator torque (pu)	1
Rated generator line voltage (pu)	1
Generator inductance in the d frame (pu)	0.7
Generator inductance in the q frame (pu)	0.7
Generator stator resistance (pu)	0.01
Flux of the permanent magnets (pu)	0.9

As it can be noticed from (1)- (4), C_p varies as a function of both the TSR and the BPA. For every fixed BPA there is a corresponding $C_p - \lambda$ curve each has a peak C_p value corresponding to an optimum TSR. Maximum C_p is achieved at optimized rotational speed ω when β is equal to zero [10].

2) Permanent Magnet Synchronous Generator (PMSG):

Variable speed direct driven PMSG wind turbines have gained increasing interest over the externally excited synchronous machine due to a significant reduction in magnet prices and magnetic material characteristics improvement. Variable-speed operation of a WTES has many advantages such as rapid response to wind speed & torque variation, causing less wear and tear on the tower and other components in the drive train. Variable-speed systems can also increase the production of the energy and reduce the fluctuation of the power injected into the grid [23]. A dq model of PMSG has been developed using equations (5)- (7) found in [24].

$$v_d = R_a i_d + L_d \frac{\partial i_d}{\partial t} - \omega L_q i_q \quad (5)$$

$$v_q = R_a i_q + L_q \frac{\partial i_q}{\partial t} + \omega \varphi_f + \omega L_d i_d \quad (6)$$

$$T_e = \frac{3}{2} \rho i_q \left((L_q - L_d) i_d + \varphi_f \right) \quad (7)$$

3) Three phase Diode Rectifier

For grid connected PMSG WT, generator's output voltage and frequency must be maintained within certain values to ensure proper grid interconnection. Since the PMSG output power is of fluctuating nature due to wind speed variability, power electronic converters are utilized to overcome such problems. Three phase diode bridge rectifier has been used for AC-DC conversion of the generator output power.

4) Boost Converter

A boost converter has been added in the DC link to extract maximum power from the WT at any given wind speed as well as expand its scope of low speed operation. Using the ORB technique for MPPT, an optimal relation between booster converter inductor current i_b versus boost converter capacitor DC voltage v_b can be found [19]. This is true as v_b is proportional to the PMSG electromotive force, and the latter is proportional to the rotational speed. By sensing the DC voltage v_b and using the optimal relation between v_b and i_b , the chopper circuit extracts maximum power from the PMSG at any wind speed. Although this method requires many offline tests, it accounts for turbine efficiency and takes into consideration the total power converters losses.

5) Three phase PWM VSI

A current regulated PWM VSI maintains the boost converter output voltage (DC link voltage) at a fixed value by balancing the input and output power at the dc-link. The PWM VSI employs two control loops, the inner loop is for the grid current control while the outer loop is for the DC link voltage control. Decoupling the grid currents in the dq axis frames provides means for controlling the active grid current at unity power factor by setting the q -axis current to zero.

B. System Behavior for Voltage Dips and LVRT Capability:

The system in figure (2) has been studied for several grid voltage dips of 30%, 60% and 90% at 0.4, 0.8 and 1.2 s to demonstrate the impact on the system elements and the simulation results are shown in figures (3)- (9). All simulation results used in the analysis are carried out using Simulink-Matlab software. During the voltage dip incidence, the grid power will fall in response to the voltage dip while the PMSG will continue to extract maximum power from the wind turbine through the boost converter as seen from figures (5) and figure (6). Since the grid power has fallen to very low value, the power extracted from the wind will be transformed into stored energy in the DC link capacitor. As for figure (3) and figure (7), grid voltage dips cause a rapid rise in the DC link voltage, reaching almost to double the normal voltage which the capacitor can tolerate when a 90% dip occurs. The rise level depends on the capacitor size, dip voltage duration and network effective impedance, which can be more than just double the normal capacitor operating voltage. The DC link voltage rise accompanies more voltage stresses on the PWM VSI as seen in figure (7) while the diode bridge rectifier suffers from neither voltage nor current stress as found in figure (8) and figure (9).

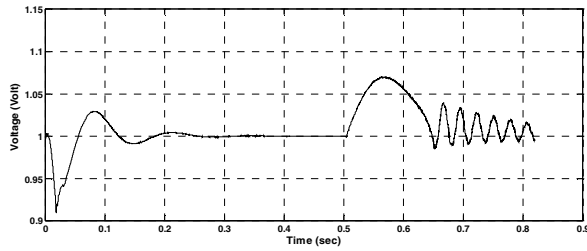


Figure 11: DC link voltage at 90% voltage dip with magnetic amplifier

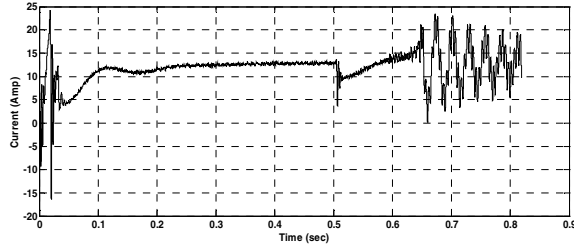


Figure 12: DC link current at 90% voltage dip with magnetic amplifier

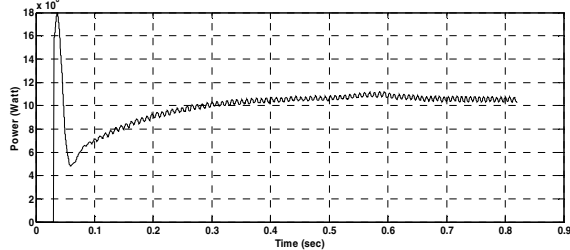


Figure 13: PMSG active power at 90% voltage dip with magnetic amplifier

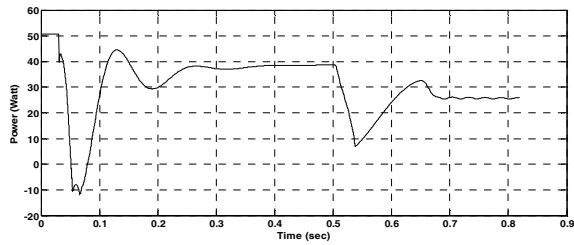


Figure 14: Grid power at 90% voltage dip with magnetic amplifier added

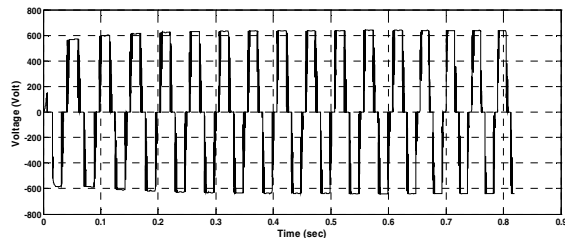


Figure 15: PMSG terminal voltage at 90% voltage dip with magnetic amplifier

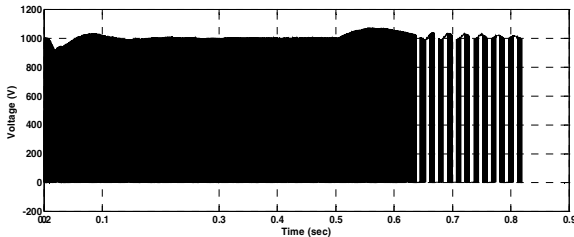


Figure 16: IGBT switch voltage at 90% voltage dip with magnetic amplifier

IV. CONCLUSION

Enhancement of low voltage ride through capability for wind turbines is becoming one of the most important issues related to the utilization and connection of wind turbines to the electrical grid. Several techniques have been adopted in literatures that ensure that grid codes are being complied in the event of grid voltage dips which, not only ensure the stability of the electrical grid post the voltage dip, but also ensure the safety of wind farm during the dip event. A novel topology based on using magnetic amplifiers in the event of grid voltage dips is demonstrated. Simulation results show that magnetic amplifier can be used to enhance the LVRT capability for direct driven PMSG WES. The application extends for the use with DFIG wind energy systems as well.

V. REFERENCES

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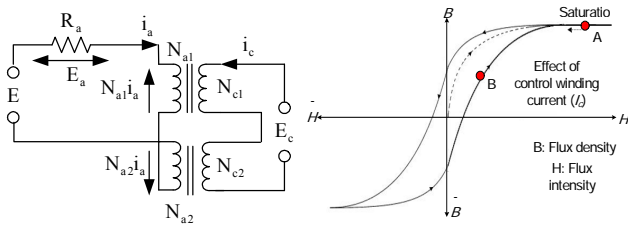
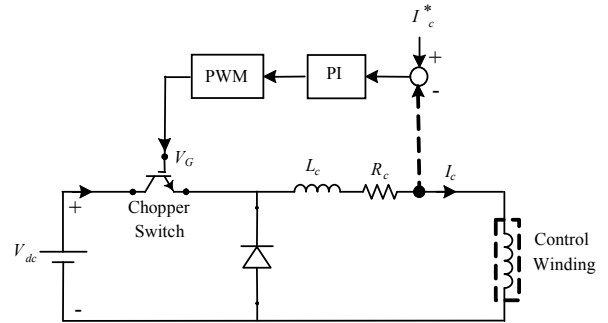


Figure 10: Connection and B - H curve of a magnetic amplifier

On the other hand, if the coupling co-efficient is small, then a large current signal is required to polarize the core and the power level at the control winding would be reasonably high[32]. Splitting the load winding into two coils connected in series opposition neutralizes the transformer action. Another modification can be made to the circuit is to include a diode in series with each of the two main windings. In this case, full utilization of the full alternating current would give higher efficiency and better waveform and reduce the time delay that can reach up to half cycle of the supply frequency.

B. Magnetic Amplifiers and LVRT Capability Enhancement:

The magnetic amplifier can be used as a method of series compensation. Changing of its control winding current changes the main winding effective impedance, thus the magnetic amplifier acts as a variable inductance if inserted between a source of emf and a load. To validate this idea, the magnetic amplifier have been used and tested for LVRT enhancement as seen in figure (11). In this configuration, each of the three phases of the PMSG is split into two windings as to avoid demagnetization of the magnetic amplifier in the negative half cycle of the supply voltage. Each winding is connected in series with a rectifying diode which helps the magnetic amplifier cores to reach saturation faster [32]. Six magnetic amplifiers have been used in the following analysis, each rating



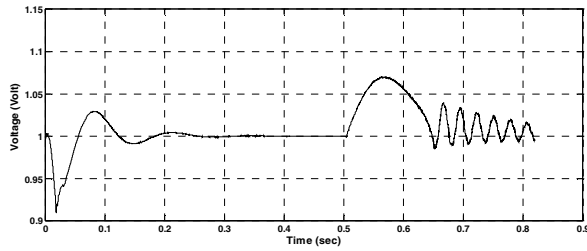


Figure 11: DC link voltage at 90% voltage dip with magnetic amplifier

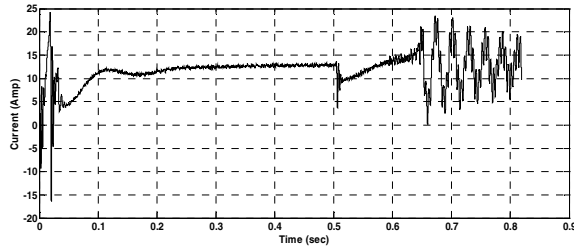


Figure 12: DC link current at 90% voltage dip with magnetic amplifier

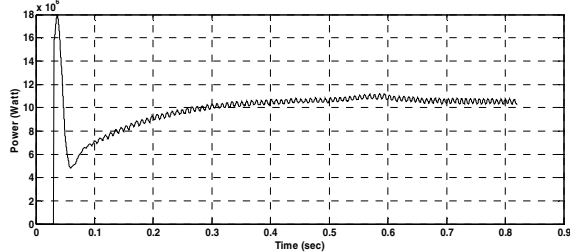


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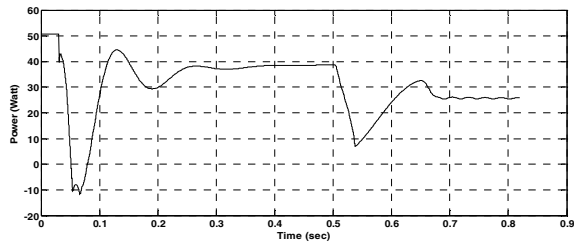


Figure 14: Grid power at 90% voltage dip with magnetic amplifier added

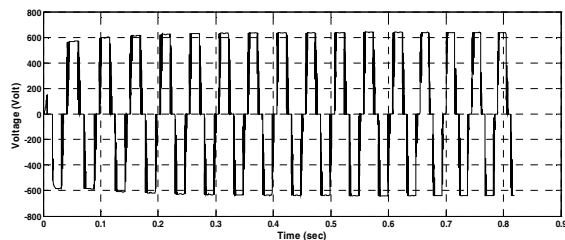


Figure 15: PMSG terminal voltage at 90% voltage dip with magnetic amplifier

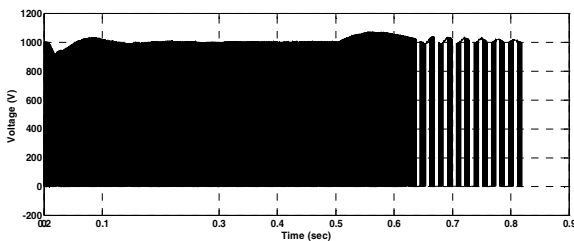


Figure 16: IGBT switch voltage at 90% voltage dip with magnetic amplifier

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